

# Power plant efficiency models and economic dispatch methods

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# *Objectives and expectations*

## Efficiency model

### Objectives

- description of market behavior
- modeling demand-supply conditions
- determination of operating and marginal costs
- estimation of pollutant emissions

### Expectations

- simplicity and minimal data requirements
- acceptable accuracy

# *Objectives and expectations*

## Economic dispatch method

### Objectives

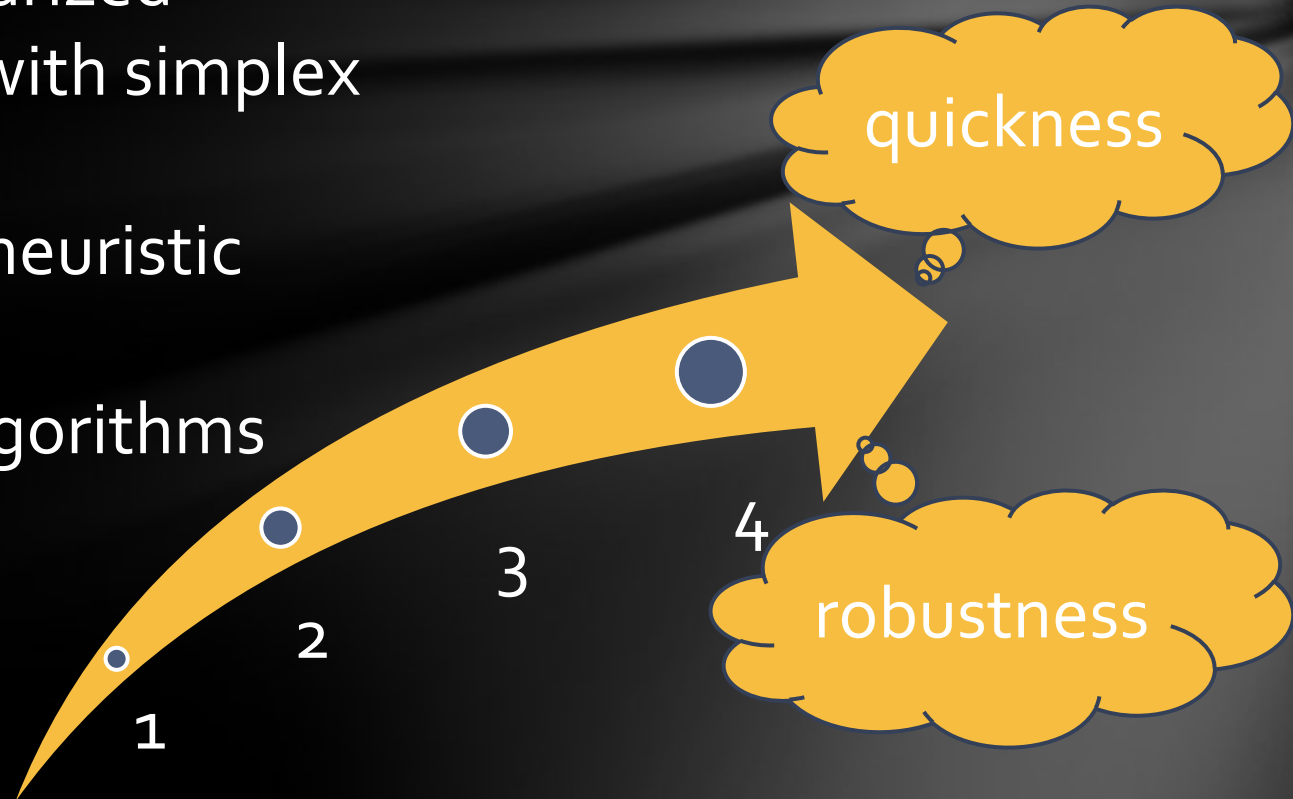
- determination of minimum operating costs
- robustness

### Expectations

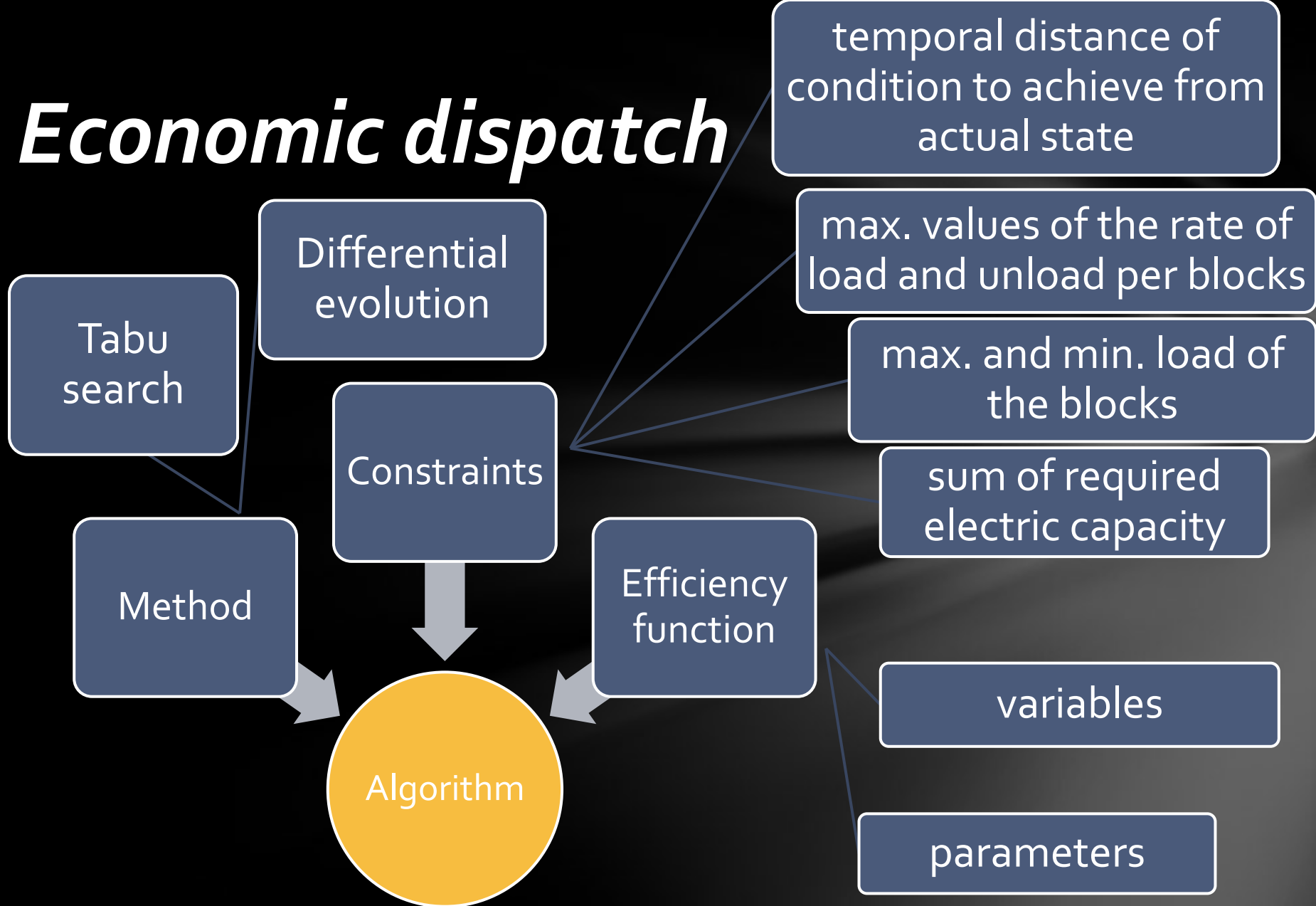
- quickness
- high hit probability
- ability to operate in real time

# *Economic dispatch methods*

1. simultaneous analytic solutions of equations
2. solution of linearized programming with simplex method
3. semi-analytic, heuristic solution
4. evolutionary algorithms

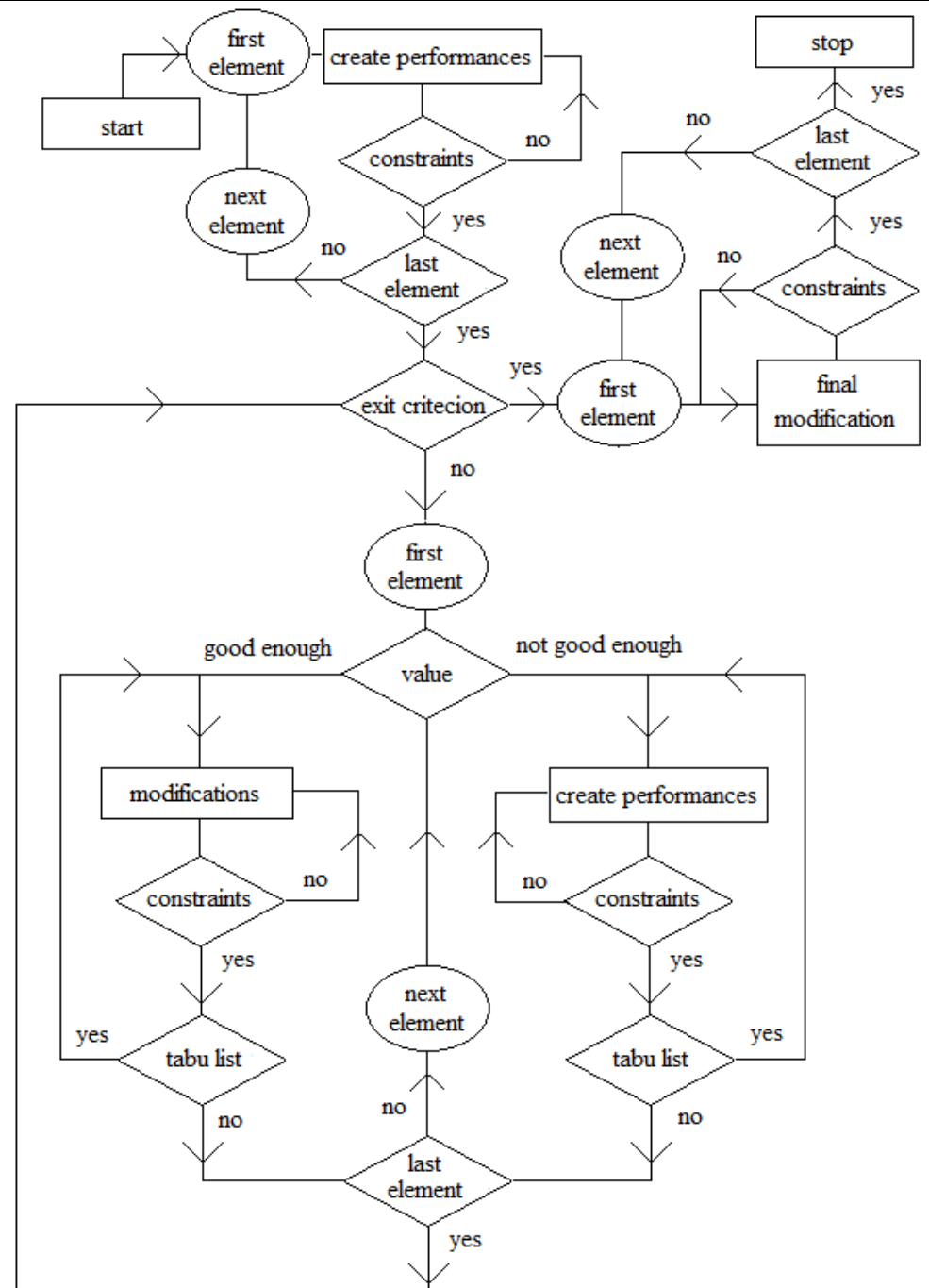


# *Economic dispatch*



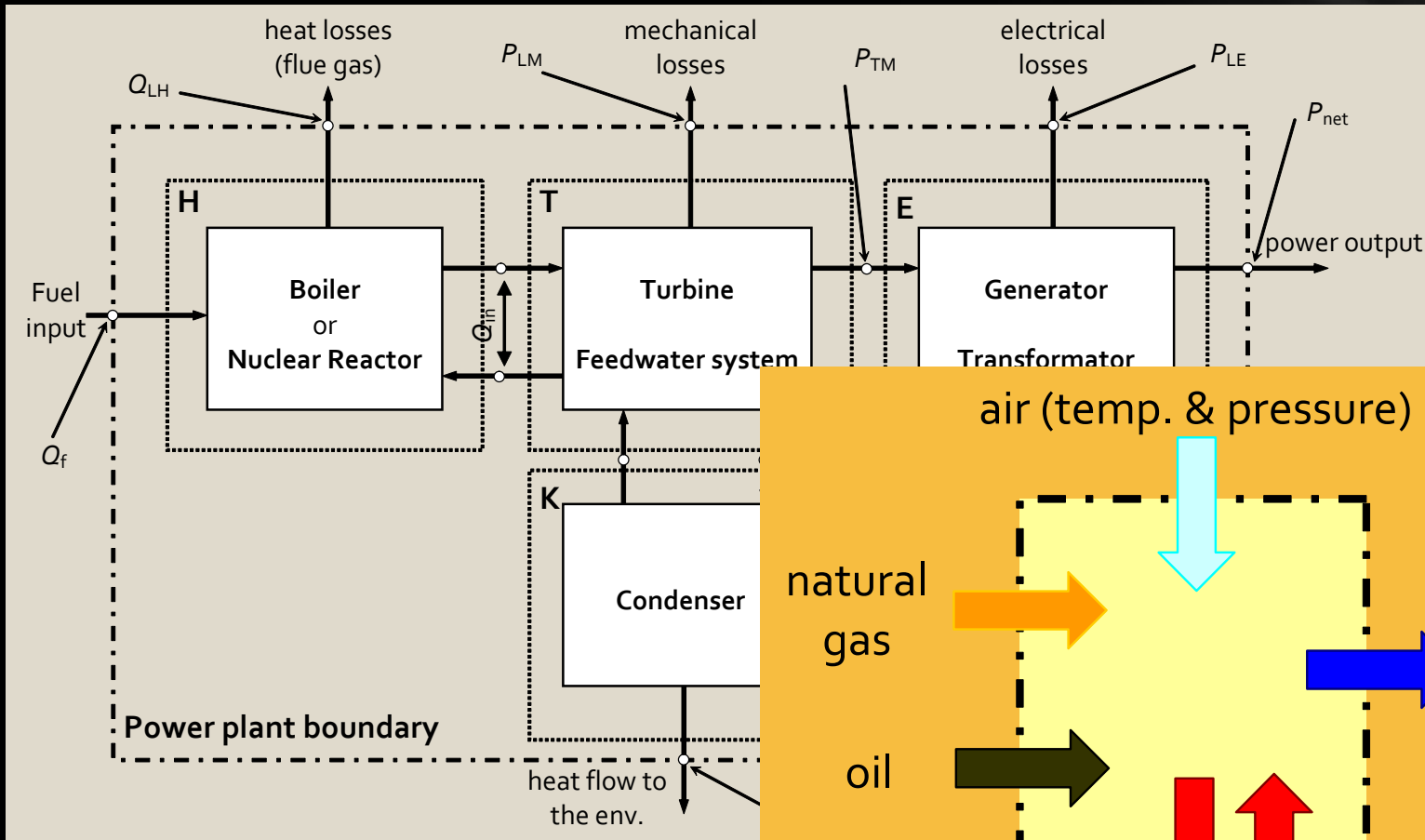
# Hybrid algorithm

Tabu search  
+  
Differential  
evolution

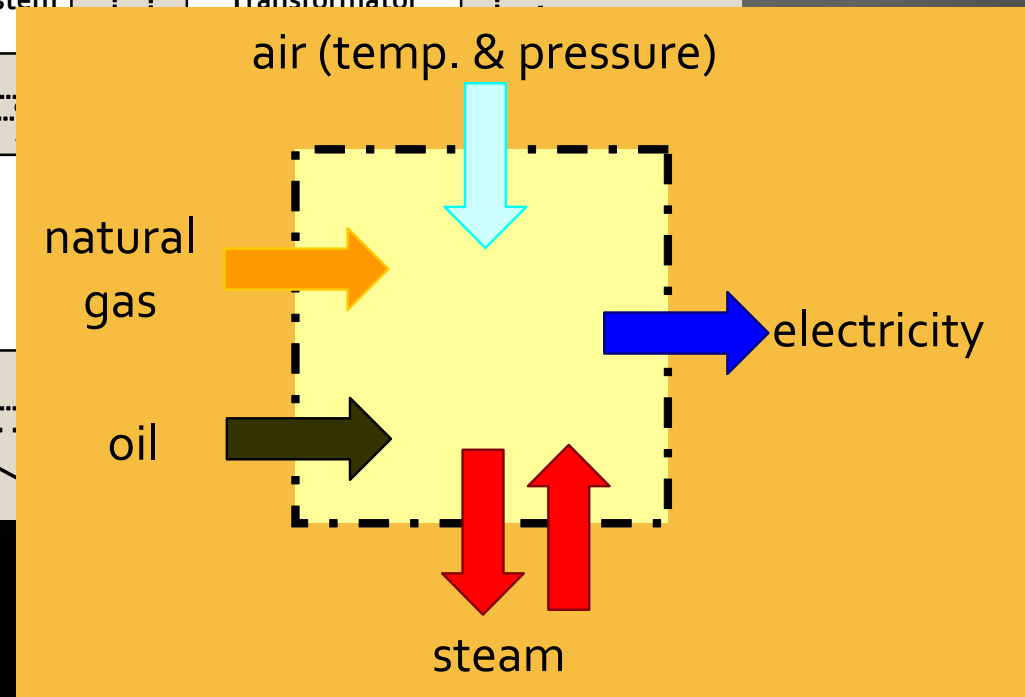


# Efficiency model

## Detailed model

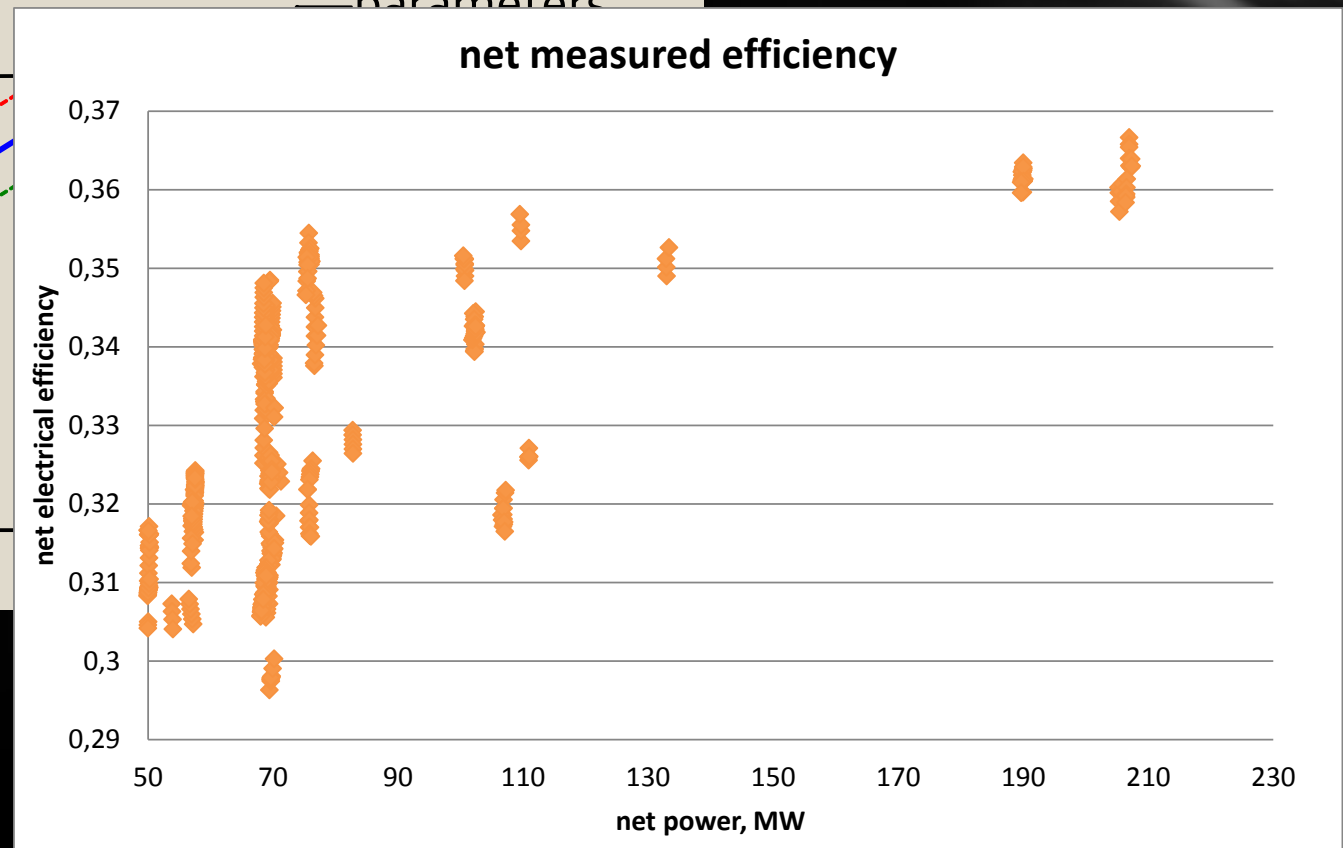
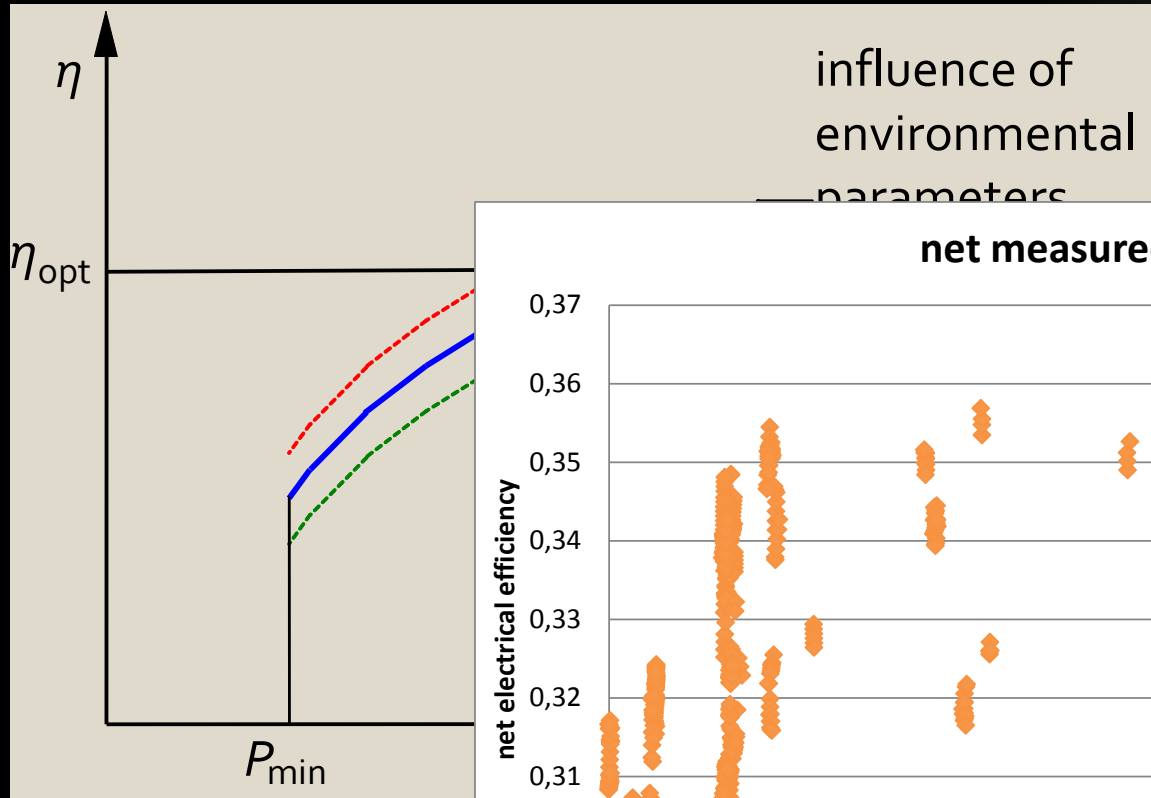


## Black box model



# Power plant efficiency

## Theoretical





# *Efficiency function*

## Base function

$$\eta P = \eta_{\text{opt}} \left\{ 1 - Xv \left( \frac{P_{\text{max}}}{P} \right) \left[ \left( \frac{1}{v^2} \right) \left( \frac{P}{P_{\text{max}}} \right)^2 - 1 \right]^2 \right\}$$

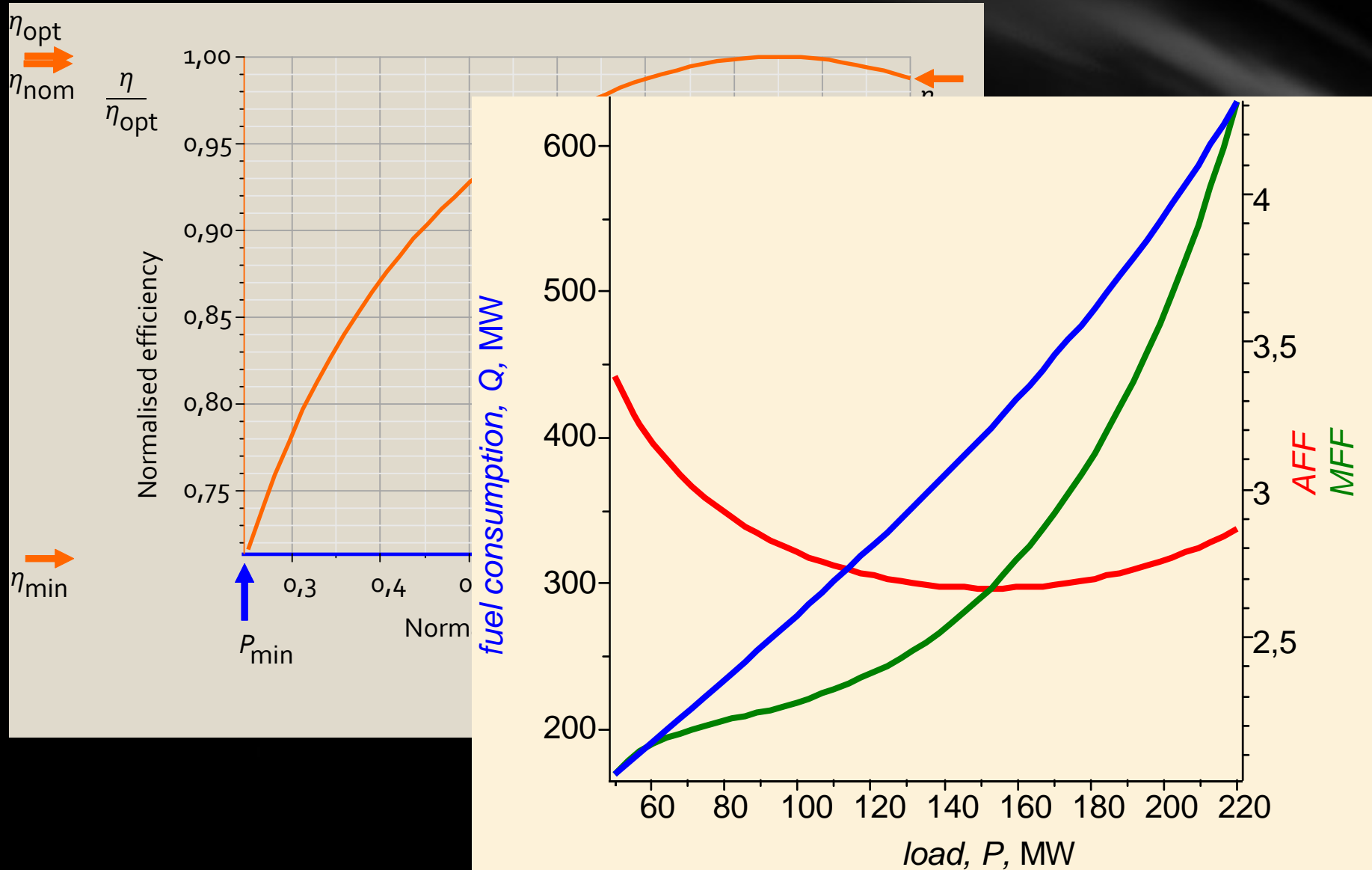
## Average fuel factor (specific fuel consumption)

$$AFF = \frac{1}{\eta P} = \frac{1}{\eta \text{ load}}$$

## Marginal fuel factor

$$MFF = \frac{d(P \cdot AFF)}{dP} = P \frac{dAFF}{dP} + AFF$$

# Efficiency function - Theory



# Efficiency function - Corrections

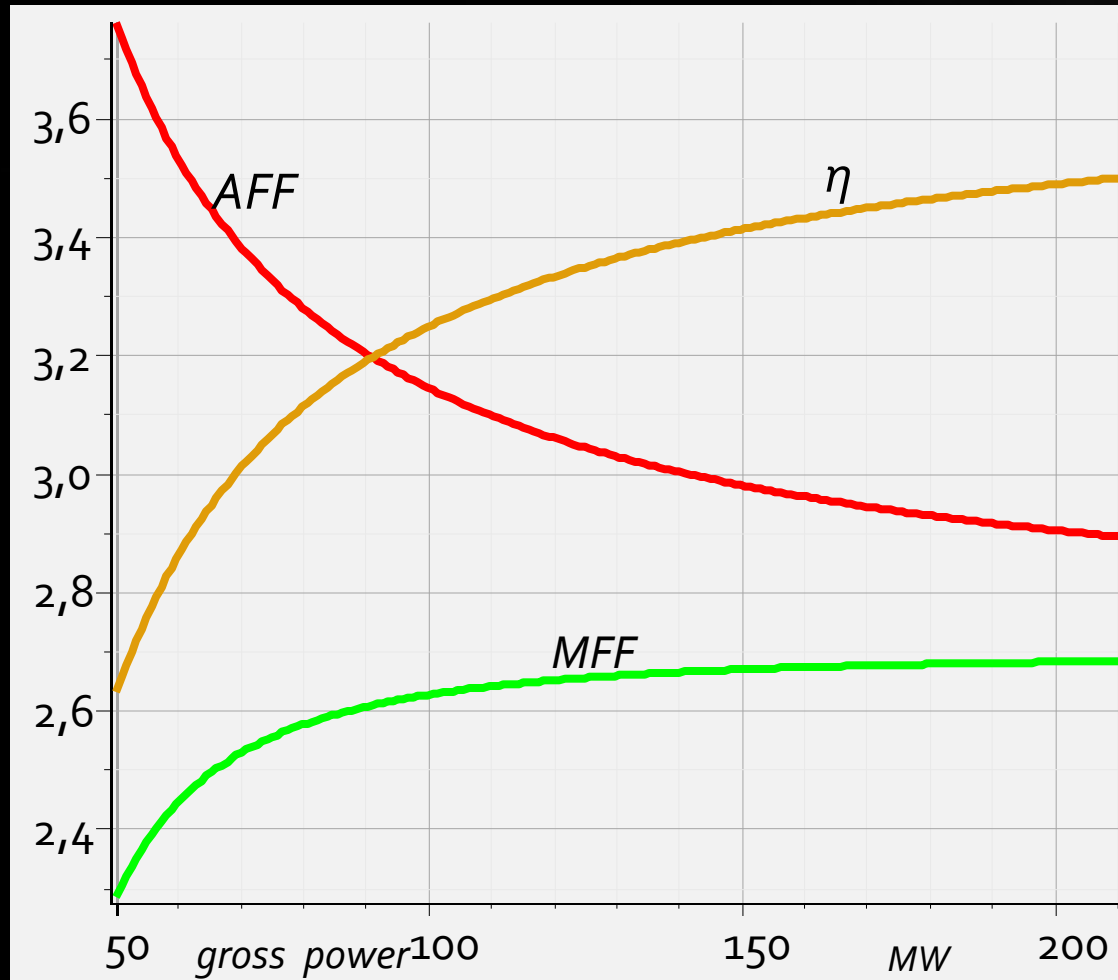
## Influencing factors (condensing unit with steam sendout)

- steam in- and outlet (mass flow only)
- air pressure and temperature
- fuel type

	Coefficient	Std. Error	t-ratio	p-value	
const	1,13984	0,0714827	15,9456	<0,00001	***
P_gross	0,00138361	7,20074e-05	19,2148	<0,00001	***
P_gross^2	-4,31467e-06	2,69952e-07	-15,9831	<0,00001	***
st_out	-0,00294359	0,000129861	-22,6672	<0,00001	***
st_in	0,000502311	0,000235524	2,1327	0,03326	**
st_out^2	7,23838e-05	5,58452e-06	12,9615	<0,00001	***
st_in^2	-2,06377e-05	1,76376e-05	-1,1701	0,24232	
t_air	0,000291736	3,67589e-05	7,9365	<0,00001	***
fuel_ratio	0,0238803	0,00169621	14,0786	<0,00001	***
p_air	-0,000872738	6,94403e-05	-12,5682	<0,00001	***
Mean dependent var	0,350585	S.D. dependent var	0,015191		
Sum squared resid	0,026942	S.E. of regression	0,005855		
R-squared	0,853143	Adjusted R-squared	0,851462		
F(9, 786)	710,9734	P-value(F)	0,000000		
Log-likelihood	2967,407	Akaike criterion	-5914,813		
Schwarz criterion	-5868,017	Hannan-Quinn	-5896,832		

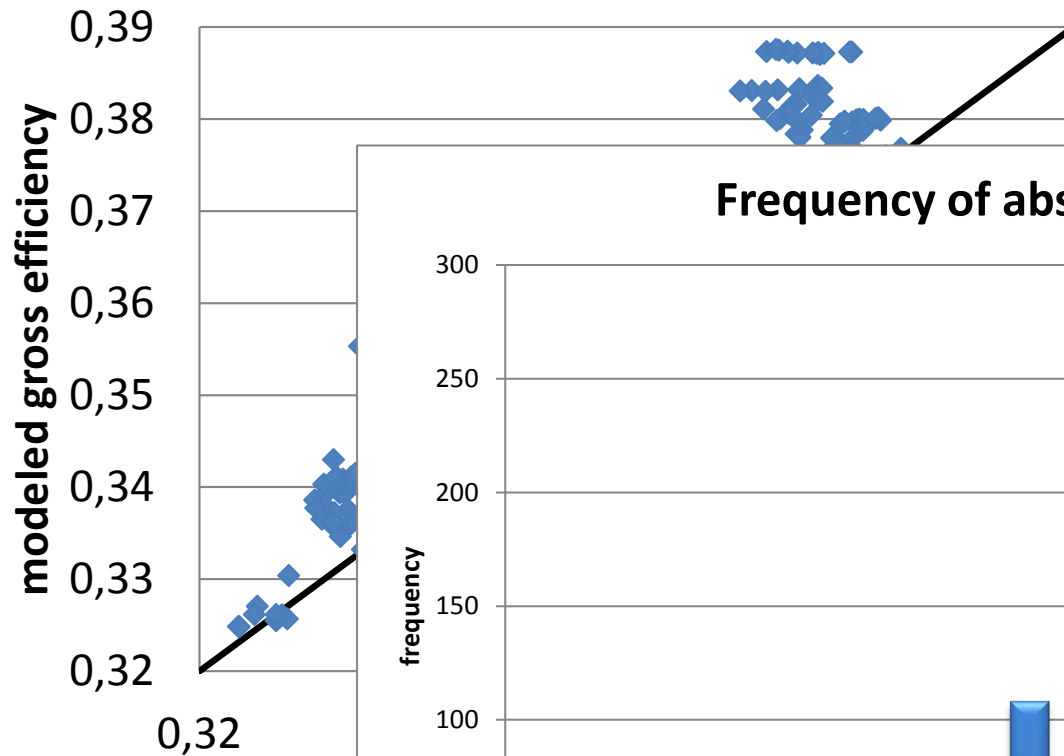
# Efficiency function - Corrections

$$\eta = \eta_{\text{opt}} \left\{ 1 - \chi v \left( \frac{P_{\text{max}}}{P} \right) \left[ \left( \frac{1}{v^2} \right) \left( \frac{P}{P_{\text{max}}} \right)^2 - 1 \right]^2 \right\} \cdot C_1 \dot{m}_{\text{steam}} \cdot C_2 T_{\text{air}} \cdot C_3 \text{fuel} \cdot C_4 p_{\text{air}}$$

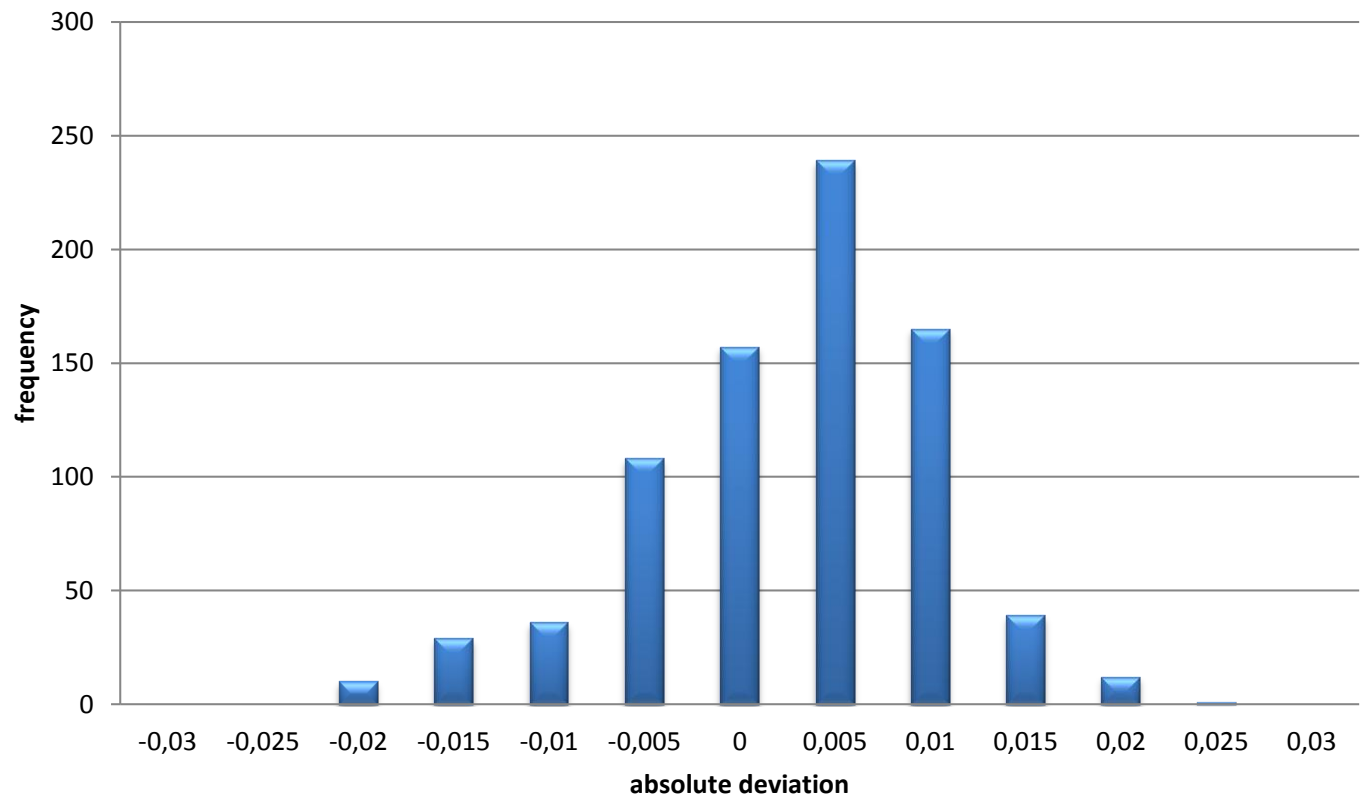


# *Efficiency function – Model validation*

**gross efficiency**



**Frequency of absolute deviations**



***Thank you for your  
attention!***